Hybrid Partitioning in Zoltan Nick Aase, Karen Devine Summer, 2011

1 Introduction

When used for partitioning, Zoltan has a wide range of algorithms available to it. Traditionally they have fallen into two categories: geometric-based partitioning, and topology-based partitioning. Each method has its own strengths and weaknesses which ultimately come down to the tradeoff between speed and quality, and the onus is placed upon the user to determine which is more desirable for the project at hand.

In our project we strived to develop a hybrid partitioning algorithm; one that attempts to take advantage of the efficiency of geometric methods, as well as the precision of topological ones. The reasoning behind this concept is that problem sets with large amounts of data may be more easily digestible by topological methods if they are first reduced into managable pieces based on their geometry.

The two subjects chosen for this project were the Recursive Coordinate Bisection (RCB) algorithm and Parallel Hypergraph partitioning (PHG). RCB is an extremely fast method of partitioning, but it can be clumsy at times when it "cuts" across a coordinate plane. On the other hand, PHG has a good understanding of the relationships between data, making its partitioning quite accurate, but it suffers from having to spend a great deal of time finding those relationships.

For further information on implementing hybrid partitioning, please see the developer's guide at http://www.cs.sandia.gov/Zoltan/dev_html/dev_hybrid.html

2 Parallel hypergraphs and geometric input

In order for Zoltan to support hybrid partitioning, it is necessary to properly and frequently obtain, preserve, and communicate coordinate data. The first step that needed to be taken was to modify PHG to support coordinate information. Hypergraph objects carry a substantial amount of data already, but we had to add an array of floating point values to store the coordinates. Currently, when a hypergraph is built and geometric information is available from the input, each vertex will have a corresponding subset within the array defining its coordinates; that is, $\forall v_x \in H: \exists C_x = \{c_0, c_1, ..., c_{n-1}\}$, where v_x is an arbitrary vertex in the hypergraph H, C_x is its corresponding coordinate subset, and n is the number of dimensions in the system. In this way, Zoltan can treat each coordinate subset as an element of that vertex

3 PHG, MPI and 2-dimensional representation

PHG is interesting in that multiple processors can share partial data that describes the properties of hyperedges and vertices. This sort of system can be represented in a 2-dimensional distribution similar to Table 1. A populated field represents that a processor on the y-axis has data related to the vertex on the x-axis. In this example, you can see that processor P_0 and P_2 share data describing vertices v_0 and v_2 .

Processor	v_0	v_1	v_2
P_0	х		х
P_1		х	
P_2	х		х

 Table 1:
 Before communication

Using Message Passing Interface (MPI) communicators, it is possible to communicate with processors by column. We use an MPI_Allreduce call to collect data from each processor, which groups them into a usable form. Consider Table 2.

Processor	v_0	v_1	v_2
P_0	х		
P_1		х	
P_2			х

 Table 2:
 After communication

This same sort of operation is performed with weight data, so implementing it on coordinate data was simply another step in setting up PHG to support coordinate information from the input. Afterwards the entirity of a vertex's data will be unique to a single processor, with the number of global vertices $= \sum_{i=0}^{numProc-1}$ (number of local vertices_i).

4 Matching

There are several matching methods already native to Zoltan and specific to PHG, but we needed to create a new method in order to use RCB on the hypergraph data. Before the actual matching occurs several specialized callbacks and parameters are registered. Doing this is crucial if RCB and PHG are to interface properly with each other.

The next task is to physically call RCB. It was easy enough to send PHG data to RCB as we simply used the Zoltan_LB_Partition wrapper, not unlike other standard load balancing partitioners. However, getting matchings *back* from RCB to PHG was another matter entirely. Thanks to Dr. Devine's work, we were able to ostensibly comondeer one of RCB's unused return values: since all matching algorithms conform syntactically to the afforementioned load-balancing wrapper, there are some arguments and/or values that are never used depending on what data that partitioner needs In the case of RCB, the return value ***export_global_ids**, which is defined in its prototype, was never actually computed. Dr. Devine was able to rewire RCB so that, when using hybrid partitioning, it would return the IDs of the matchings we need for each hypergraph (which are referred to in the matching procedure as *candidates*).

This new matching procedure is similar to PHG's agglomerative matching, whereby candidate vertices are selected to represent groups of similar vertices. These candidates then make up the standard vertices in the resultant coarse hypergraph. The major difference is that standard agglomerative matching determines its candidates by the connectivity of vertices to one another; the more heavily connected a subset of vertices is, the more likely they will share the same candidate. Using RCB means making the assumption that related vertices will be geometrically similar: recursive geometric cuts will be more likely to naturally bisect less connected parts of the hypergraph, and the vertices that are members of the resulting subdomains will share the same candidates. Given RCB's track record, this method should be significantly faster than the agglomerative matching.

5 Reduction factor

When using hybrid partitioning, the user passes a parameter in the input file called HYBRID_REDUCTION_FACTOR, which is a number > 0 and ≤ 1 that gets passed into RCB. This parameter defines the aggressiveness of the overall procedure. This

number simply determines the amount by which the larger graph will be reduced (e.g. for the original, fine hypergraph, H_f , where the number of vertices $|V_f| == 1000$, and a reduction factor of f == 0.1, the coarse hypergraph, H_c , will have $|V_c| == 100$ vertices).

This gives the user more control over the balance between quality and efficiency.

6 Results

We ran experiments primarily with 2 and 128 processors on the Odin cluster at Sandia National Labs, though there were brief, undocumented forees with 16 and 32 processors as well. Odin has two AMD Opteron 2.2GHz processors and 4GB of RAM on each node, which are connected with a Myrinet network [1]. The partitioning methods used were RCB, PHG, and hybrid partitioning with a reduction factor of 0.01, 0.05, and 0.1. Each run went through 10 iterations of the scenario. The runs with 128 processors were given 5 different meshes to run on, whereas the 2 processor runs only ran on the 4 smaller meshes, as the cluster was undergoing diagnostics at the time of the experiments.



Figure 1: Runtimes on 128 processors

You can see from Figure 1 and 2 that at 128 processors the hybrid methods are mainly slower than PHG and less accurate than RCB: both results are the inverse of what we had hoped. There was better news looking at where the processes were taking their time though:

The dramatic decrease in the matching time meant that RCB was, indeed, helping on that front.

When we ran our simulations in serial, however, we saw some very different results:

In general the hybrid times beat the PHG times, and the hybrid cuts beat the RCB cuts.

Looking at individual timers in this serial run, we can see that RCB has still drastically reduced the matching time. In addition, the slowdown in the coarse partitioning has been greatly reduced.

7 Conclusion and discussion

The parallel implementation of hybrid partitioning is obviously not functioning as desired, but we believe that there is ultimately a great deal of promise in this method. Seeing the results from our serial runs is encouraging, and it would be worth the effort to continue forward.

Perhaps it would be helpful to check for any communication issues arising between processors. The whole system could potentially drag, was a single processor waiting for a message. Additionally, Dr. Catalyurek had suggested only using RCB-based coarsening on the largest, most complex hypergraphs, and then revert to standard agglomerative matching for coarser iterations.

At this moment, there could be four different ways to use Dr. Catalyurek's method: the first, and perhaps simplest of the three, would be to hardwire in the number of coarsening levels to give to RCB. A second way would be to define a new parameter to allow the user to select the number of RCB-based coarsenings. A third would be to write a short algorithm to determine and use the optimal number of layers based off of the input. Finally, there could be an option of user input, with a default to be either of the other ways.



Figure 2: Cuts on 128 processors



Figure 3: Timing by percentage on 128 processors (UL, Shockstem 3D; UR, Shockstem 3D – 108; LL, RPI; LR, Slac1.5



Figure 4: Runtimes in serial on 2 processors



Figure 5: Cuts in serial on 2 processors

References

 U.V. Catalyurek, E.G. Boman, K.D. Devine, D. Bozdag, R.T. Heaphy, and L.A. Riesen. A Repartitioning Hypergraph Model for Dynamic Load Balancing. Sandia National Labs, 2009.

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Figure 6: Timing by percentage on 2 processors (UL, Shockstem 3D; UR, Shockstem 3D – 108; LL, RPI; LR, Slac1.5